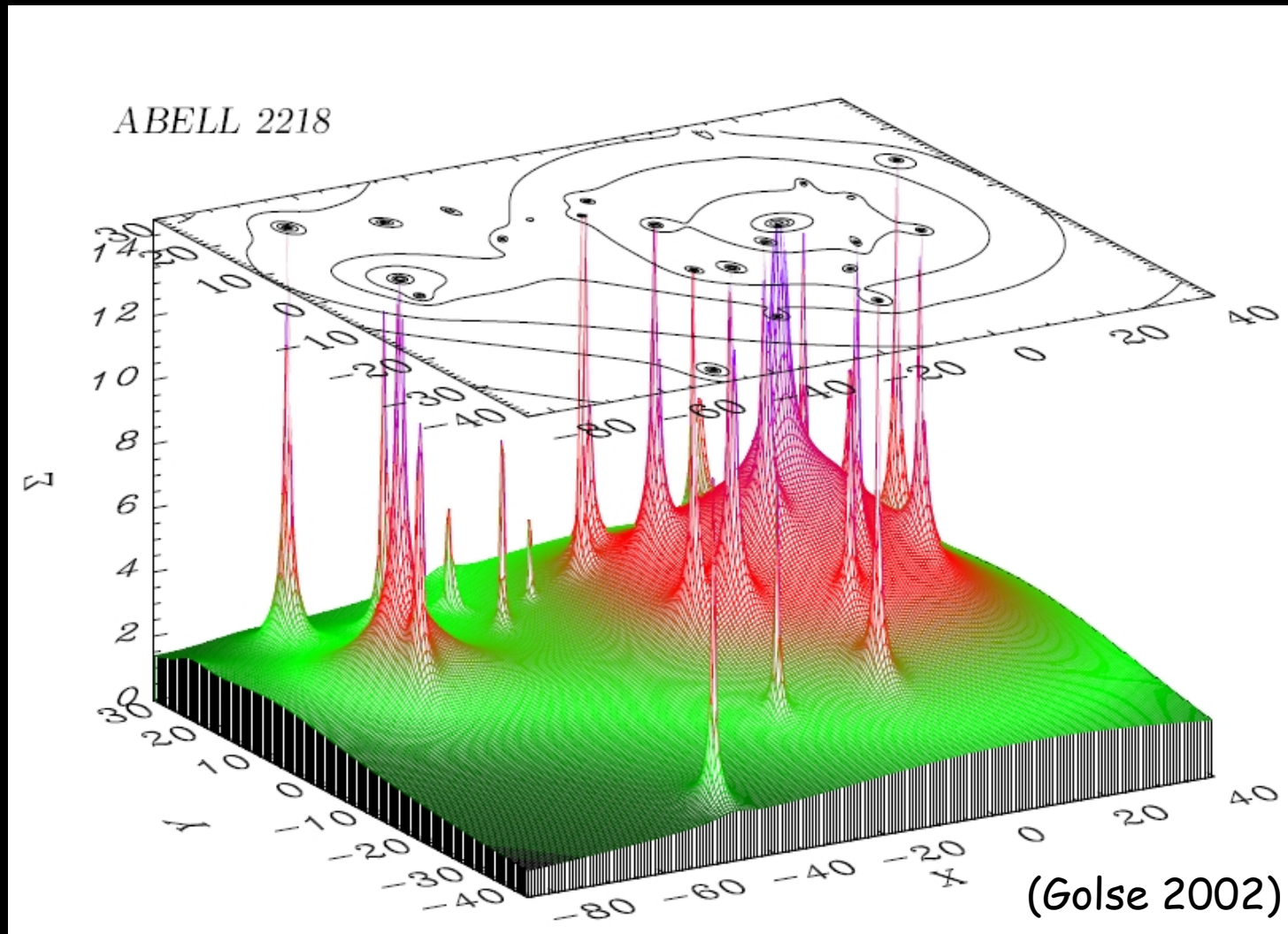


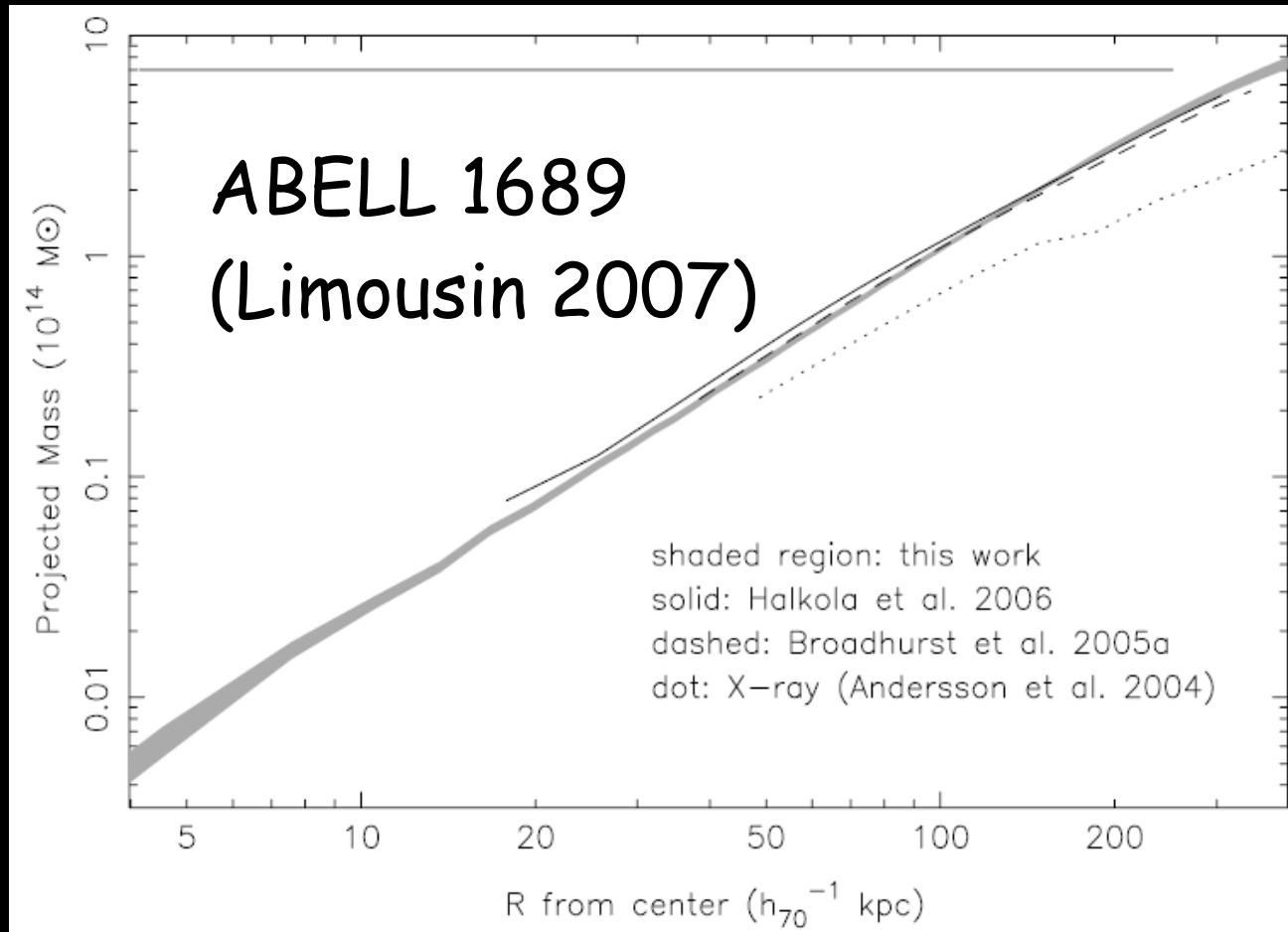
# Strong Lensing modelling techniques in Clusters of Galaxies

Eric Jullo @ OAMP.fr - MPE, Garching 2008



PhD Supervisor: Jean-Paul Kneib

# Xray - lensing mass discrepancy



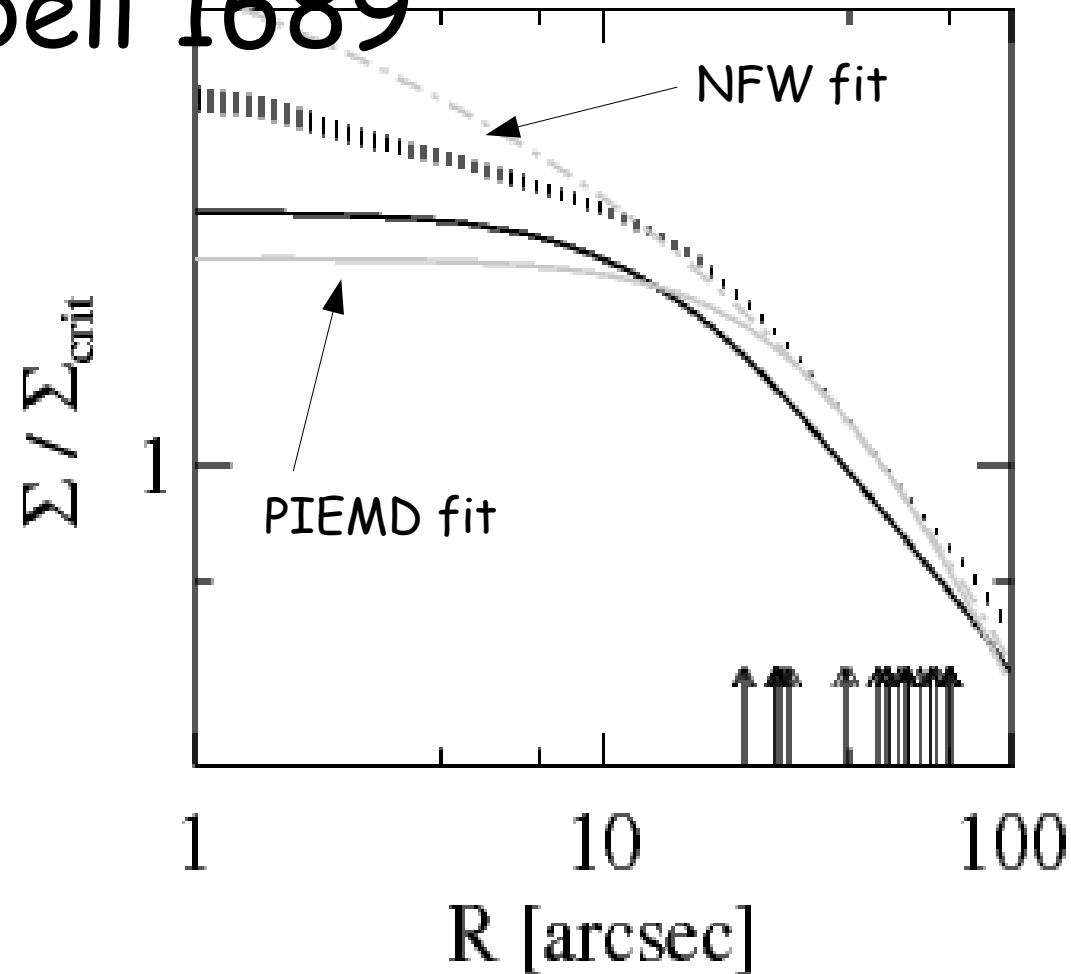
A merger along the line of sight?  
(Anderson & Madejski 2004)

# Explanation

- Bartelmann96:
  - More elliptical + More subst. = more multiple images
  - More subst. in unrelaxed clusters (merging, cf Graham & Taylor2008)
  - Xray mass of unrelaxed clusters is usually underestimated (non thermal emission, non spherical symmetry)

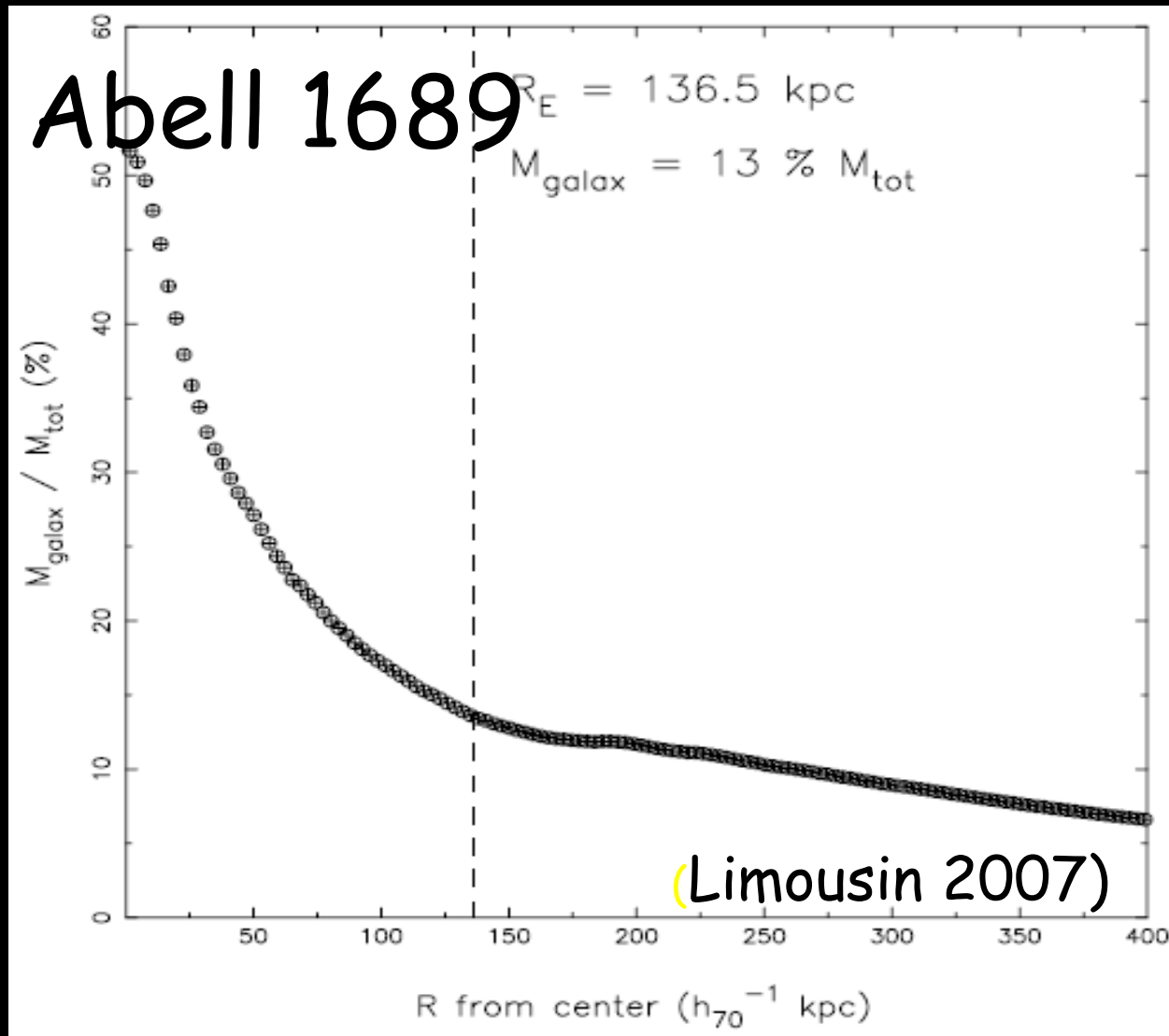
# Explanation

Abell 1689



OR missing the mass of subst. ?

# Explanation



OR missing the mass of subst.?

# How to estimate mass of subst.?

- Their degeneracies with cluster scale component(s)

# Outlines

- "Non parametric" techniques
- Parametric techniques
- Mixed technique parametric & non parametric
- Can we trust lensing mass maps?
  - Physical parameters systematics
  - Non physical parameters systematics

# SL Modeling techniques

- Lensing Parametric models are observationally and physically motivated description of DM halos
- Lensing "Non parametric" models are systematic descriptions of DM halos (grids).

They could lead (in the future) to automatic modelling ("assumption free models")?



# SL Modeling techniques

- Less parametric models are observational and physically motivated descriptions of DM (e.g. profiles).
- Lensing "Non parametric" models are systematic descriptions of DM (e.g. profiles).

They could lead (in the future) to automatic modelling ("assumption free models")?

**!! All Models are parametric !!**

# "Non parametric" techniques

## Usual approach :

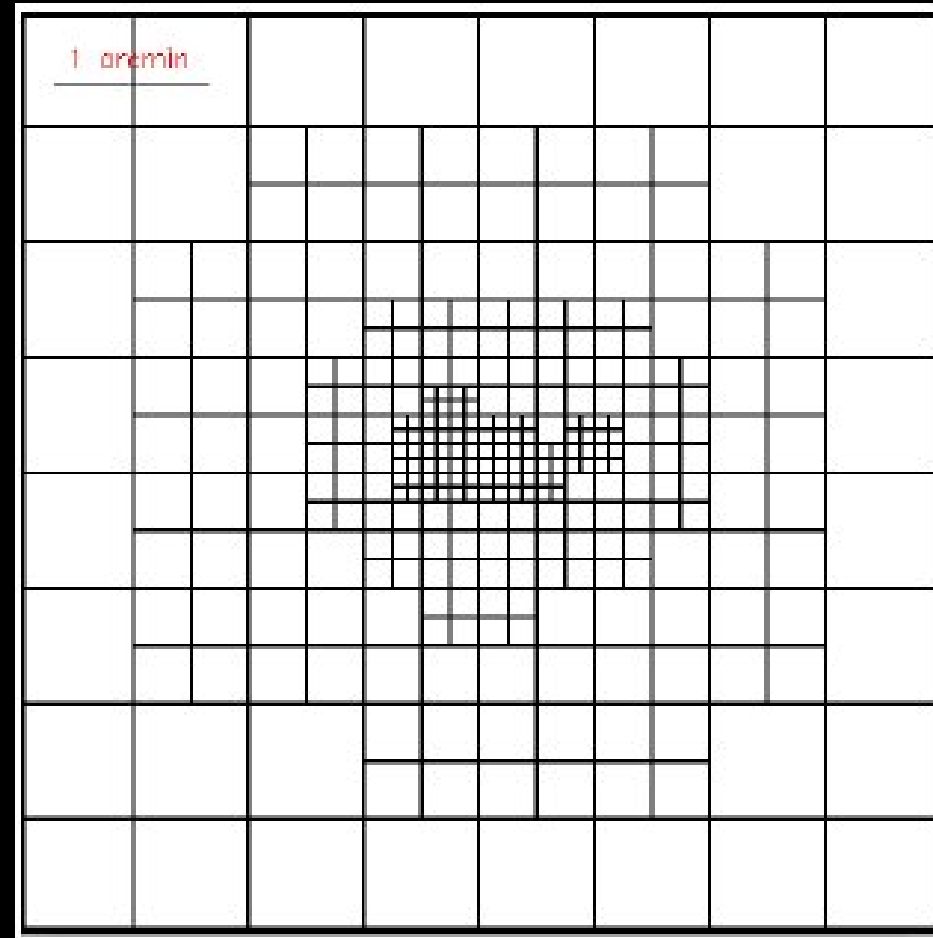
- Grid of pixels of mass or potentials (Bradač 2005)
- Compute predictions by interpolating these quantities at the position of the strong or weak lensing constraints

- Minimise  $\chi^2 = \left( \frac{\text{prediction} - \text{observation}}{\sigma_{pos}} \right)^2$

!! N free parameters > N constraints !!

- + Very flexible models
- Many solutions → Regularisation schemes

**FEW STUDIES OF SYSTEMATICS EFFECTS (Abelsalam98 rotated grid technique)**

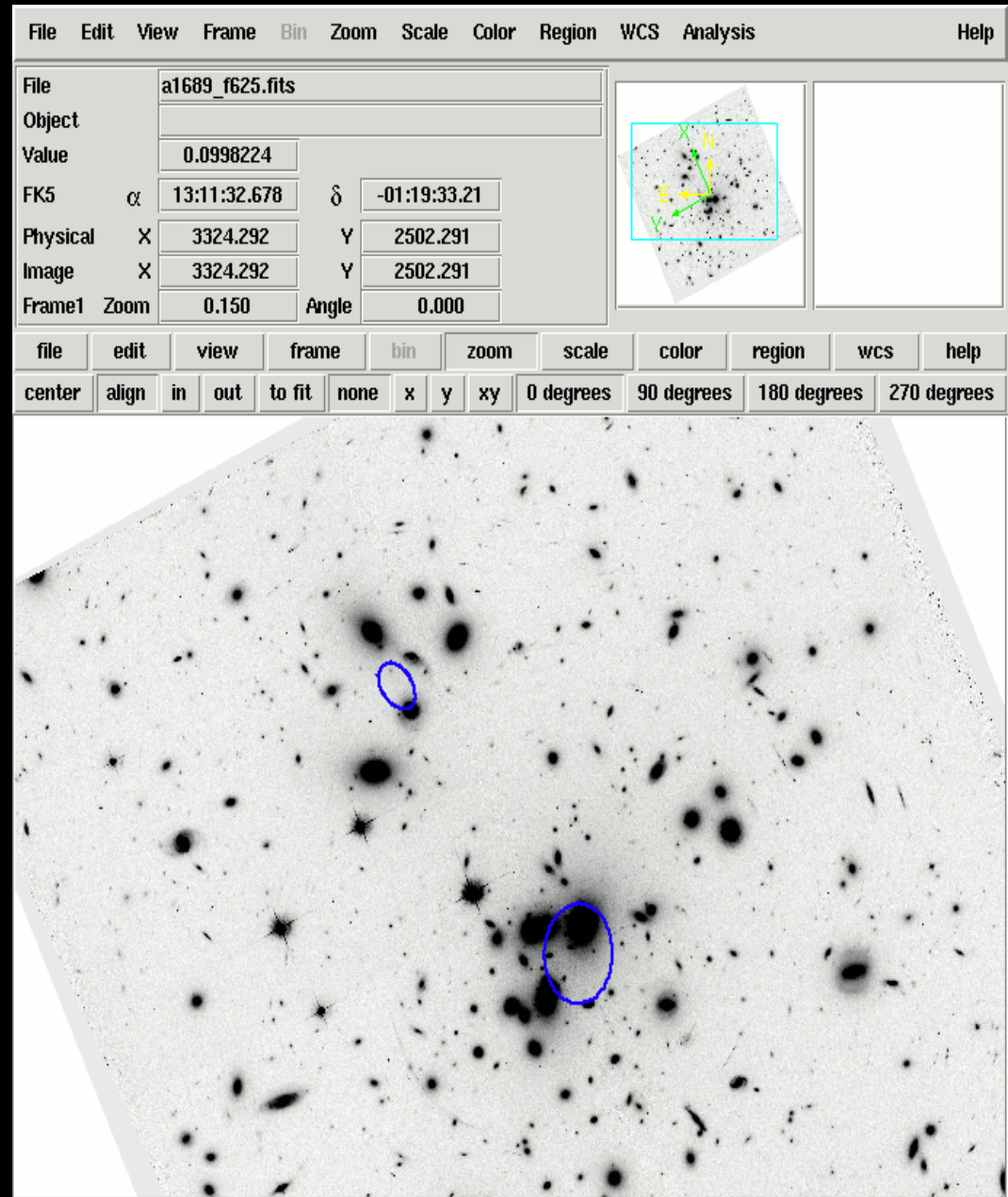


Adaptive gridding  
(Diego et al. 2005)

# Parametric techniques

Lenstool code

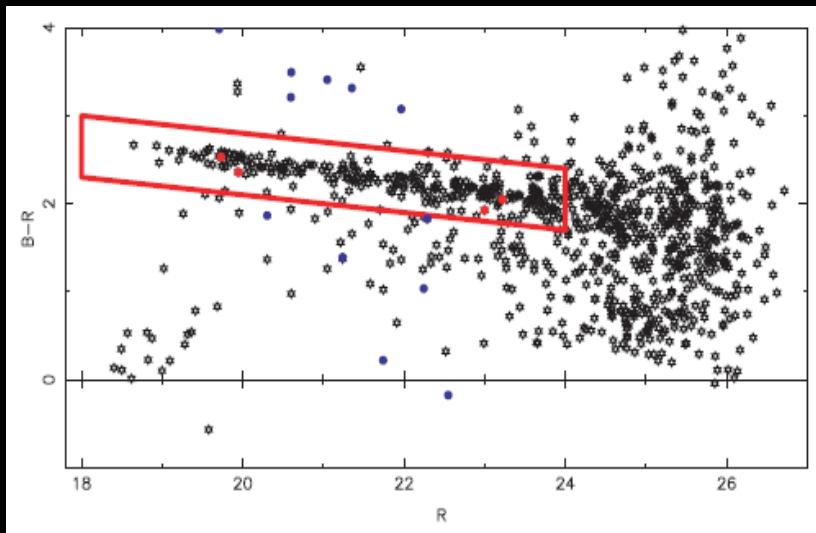
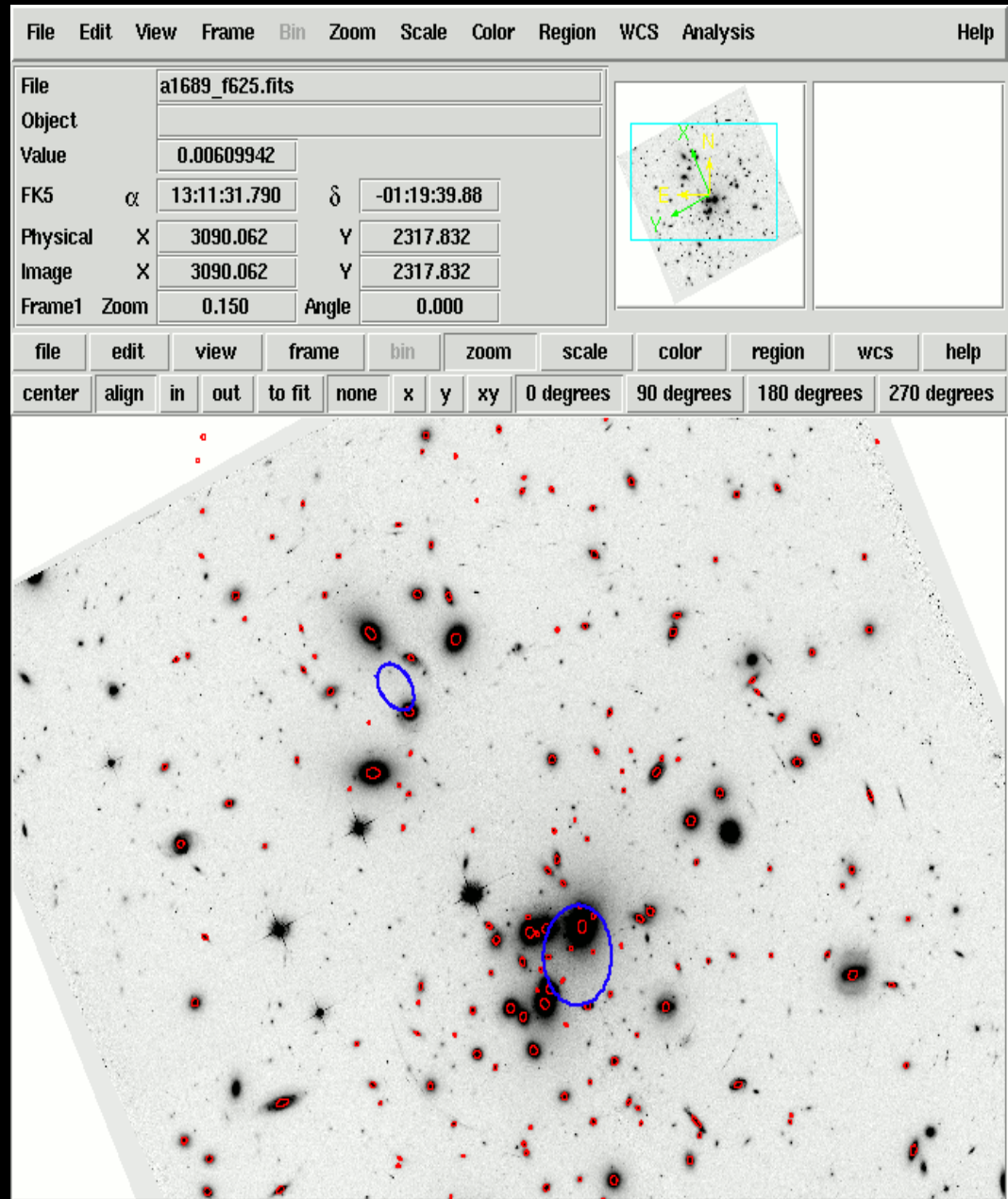
1) Place the potentials  
on the cluster



# Parametric techniques

Lenstool code

- 1) Place the potentials on the cluster
- 2) Add galaxy members



Color magnitude diagram  
(Limousin et al 2007)

# Reduce Nb of free parameters: Scaling relations

- Galaxy scale halos are described by PIEMD potentials and scaling relations

$$r_{core} = r_{core}^* \left( \frac{L}{L^*} \right)^{1/2} \quad r_{cut} = r_{cut}^* \left( \frac{L}{L^*} \right)^{1/2} \quad \sigma_0 = \sigma_0^* \left( \frac{L}{L^*} \right)^{1/4}$$

- $r_{core}^*$  is fixed
- $r_{cut}^*$  and  $\sigma_0^*$  are the 2 only remaining free parameters for the galaxy scale clumps

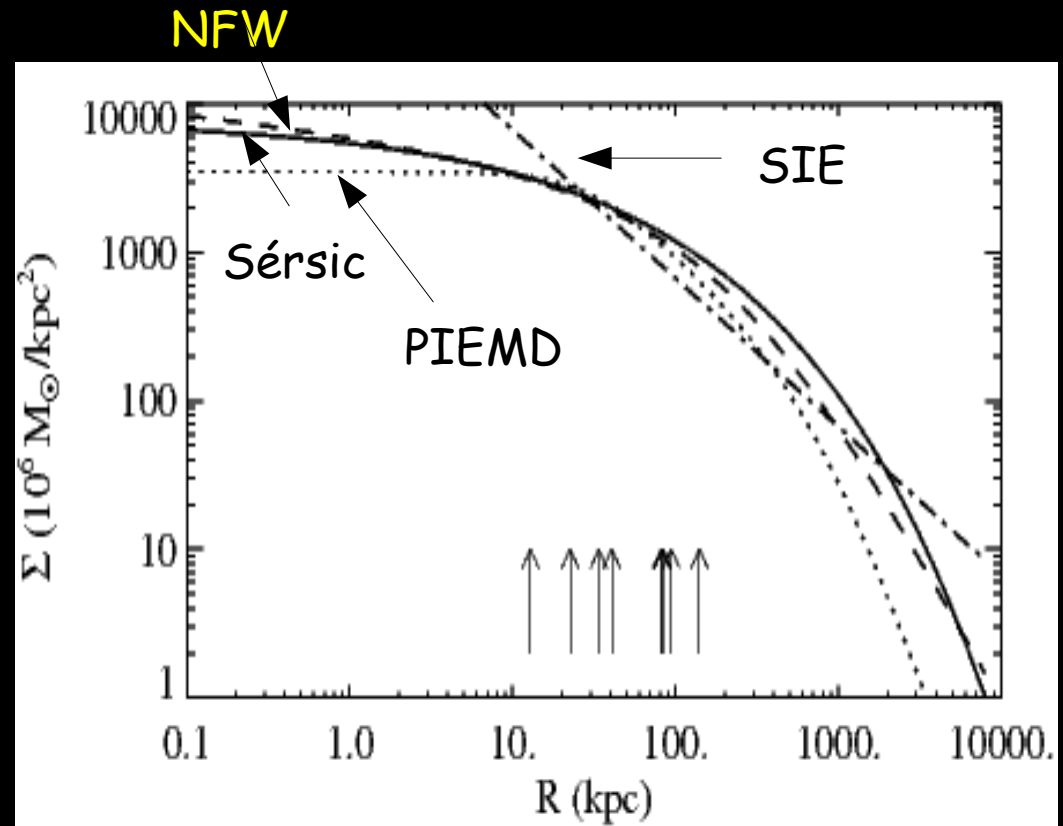
# Parametric techniques

Lenstool code

1) Place the cluster scale mass clumps

2) Add galaxy members

3) Assign a potentials to the clumps



PIEMD surface density :

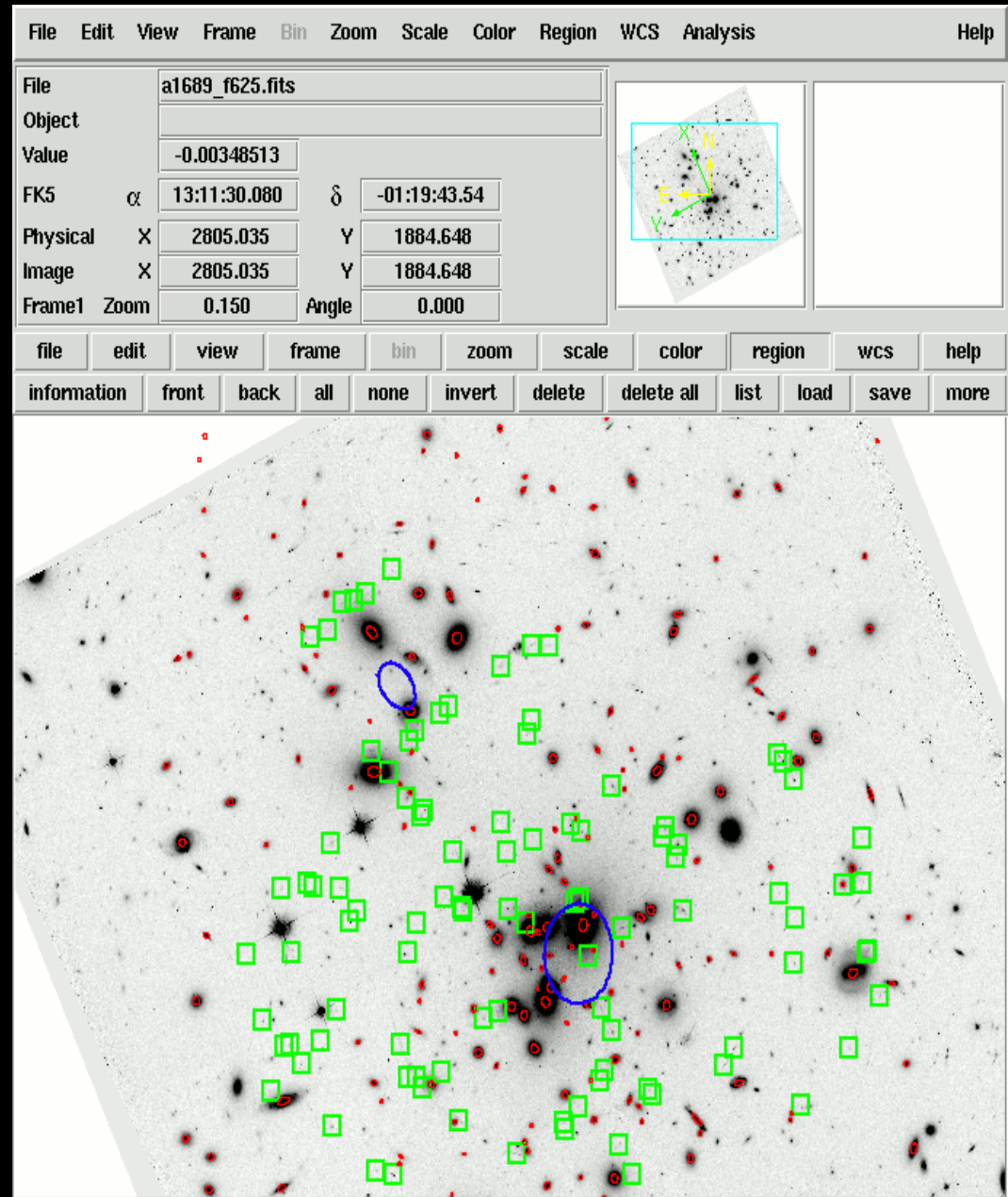
$$\Sigma(R) = \frac{\sigma_0^2}{2G} \frac{r_{cut}^2}{r_{cut}^2 - r_{core}^2} \left( \frac{1}{\sqrt{r_{core}^2 + R^2}} - \frac{1}{\sqrt{r_{cut}^2 + R^2}} \right)$$

(Jullo et al 2007)

# Parametric techniques

Lenstool code

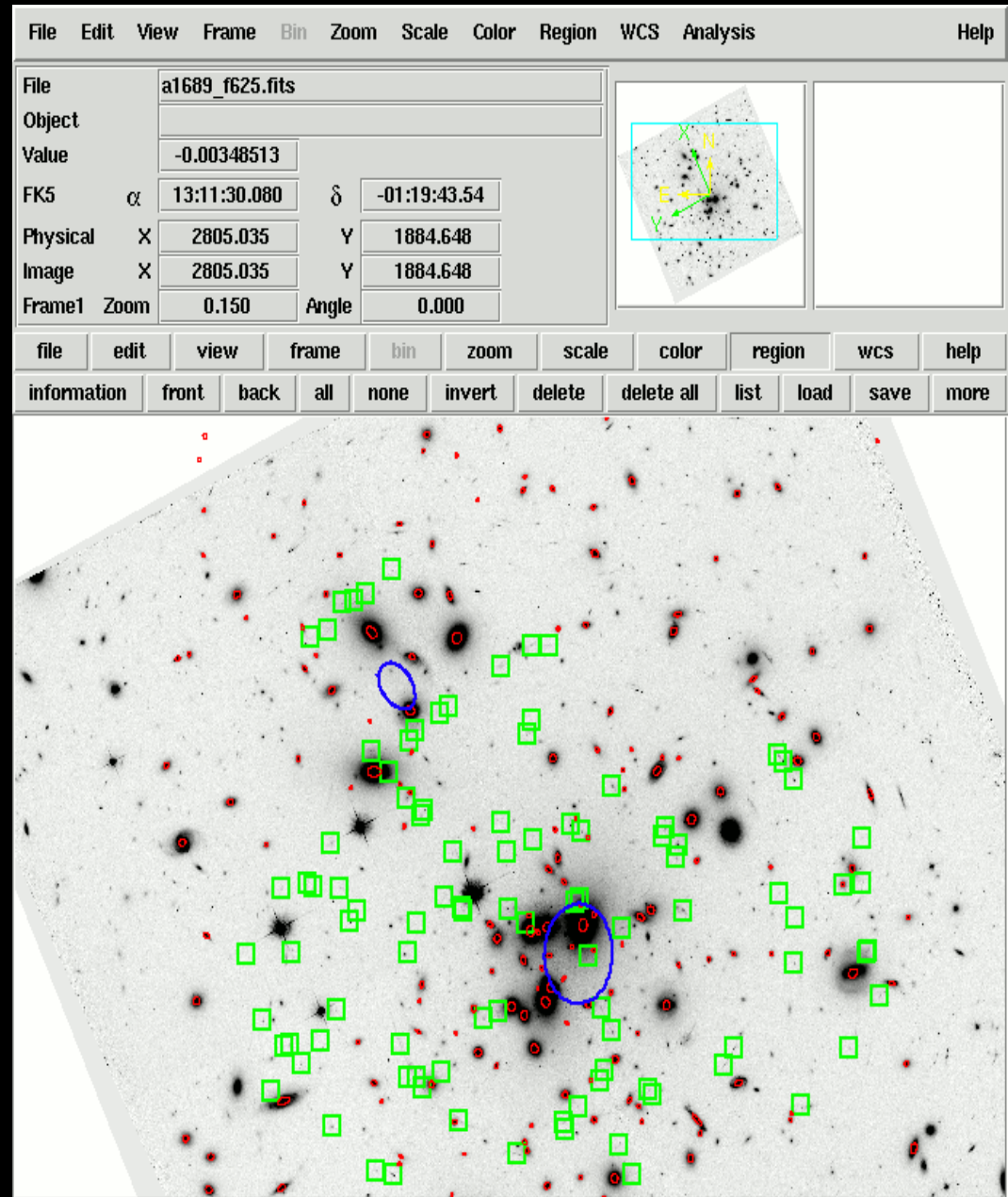
- 1) Place the cluster scale mass clumps
- 2) Add galaxy members
- 3) Assign a potentials to the clumps
- 4) Add the constraints



# Parametric techniques

Lenstool code

- 1) Place the cluster scale mass clumps
- 2) Add galaxy members
- 3) Assign a potentials to the clumps
- 4) Add the constraints
- 5)  $\chi^2 \rightarrow$  best fit model



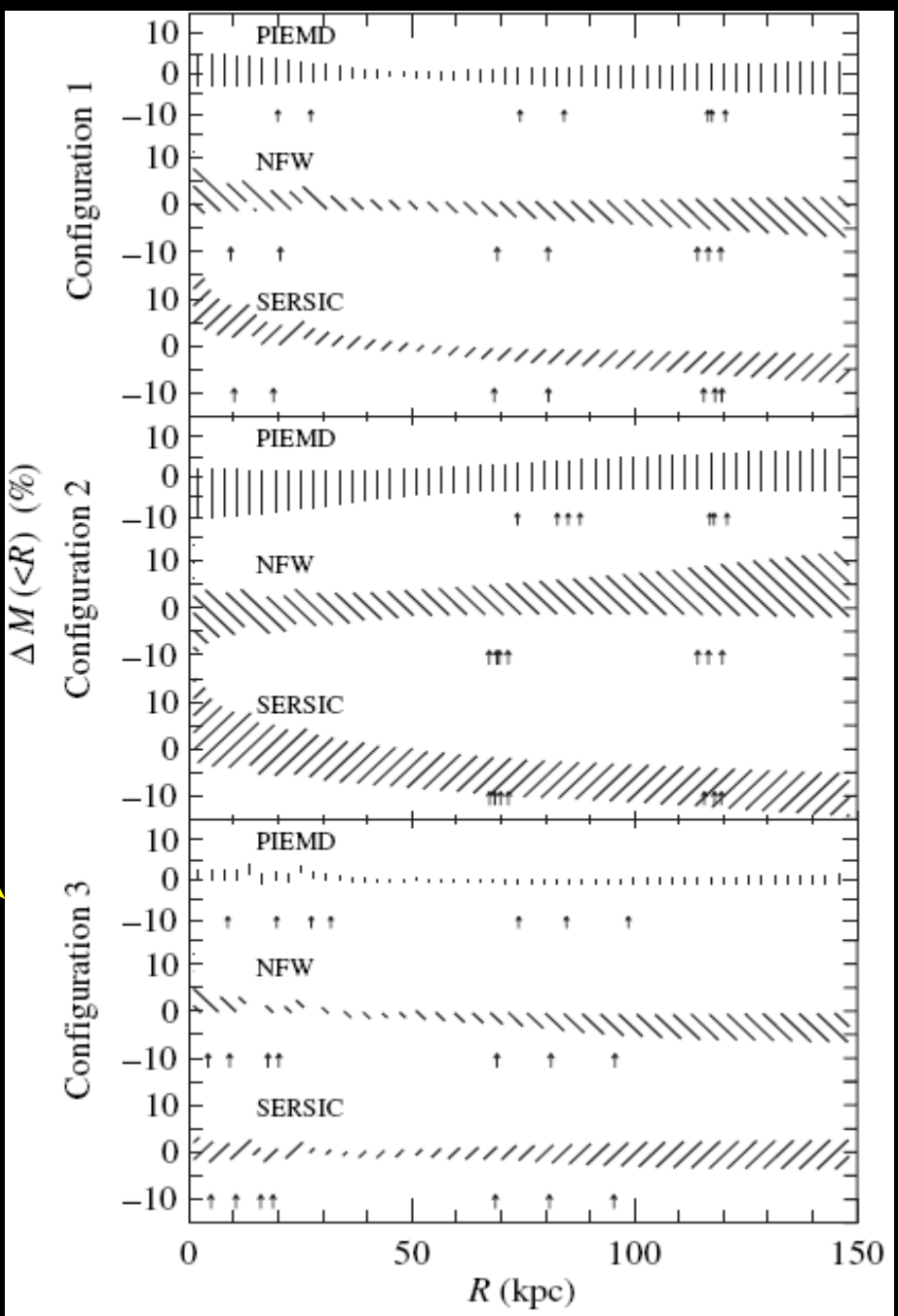


# Dependance on the SL config.

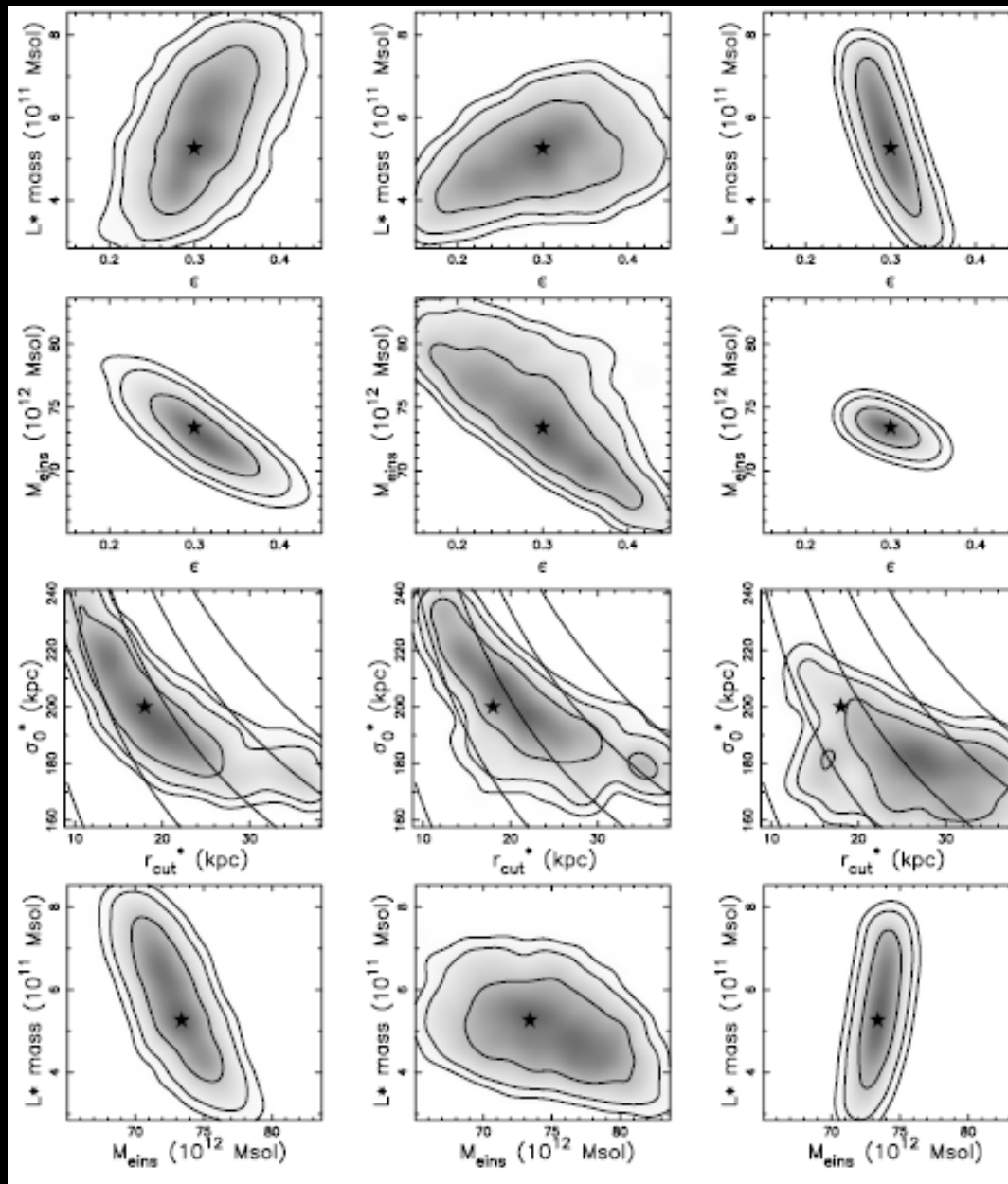
## Mass constraints

3 different SL lensing simulations with 7 images from 3 sources at redshifts  $z_s = 0.6 \rightarrow 4$   
 $z_{lens} = 0.2$

(Jullo et al. 2007)



# Degeneracies between parameters



Mass degeneracies

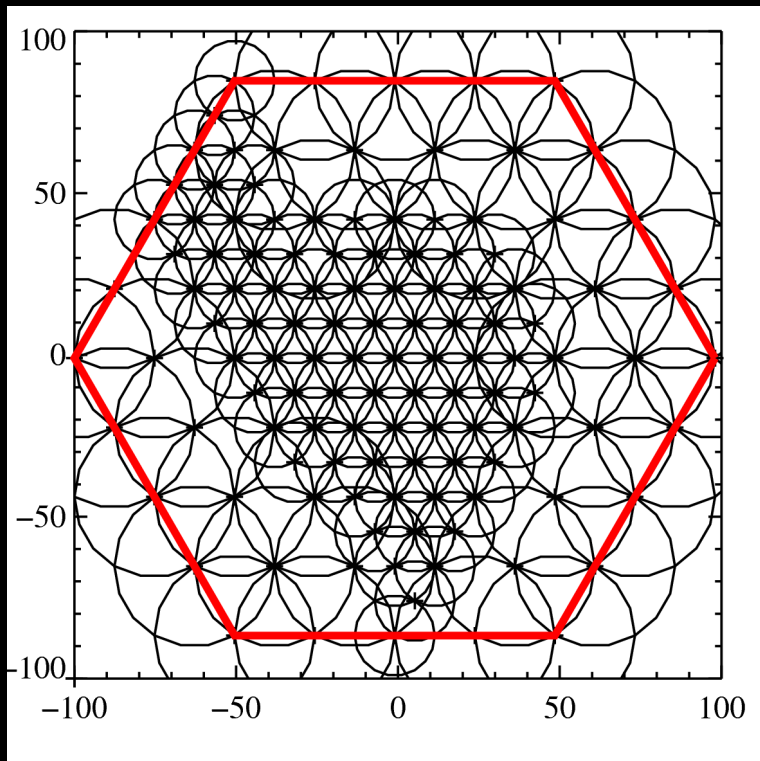
Bayesian MCMC sampler of the posterior  $\text{Pr}(\theta|D)^*$

\*Lenstool code

# Adaptative grid model

(Jullo & Kneib, submitted)

→ Multiscale-grid of 120 PIEMD clumps with free  $\sigma_0$  but fixed  $r_{\text{core}}$ ,  $r_{\text{cut}}$  and position



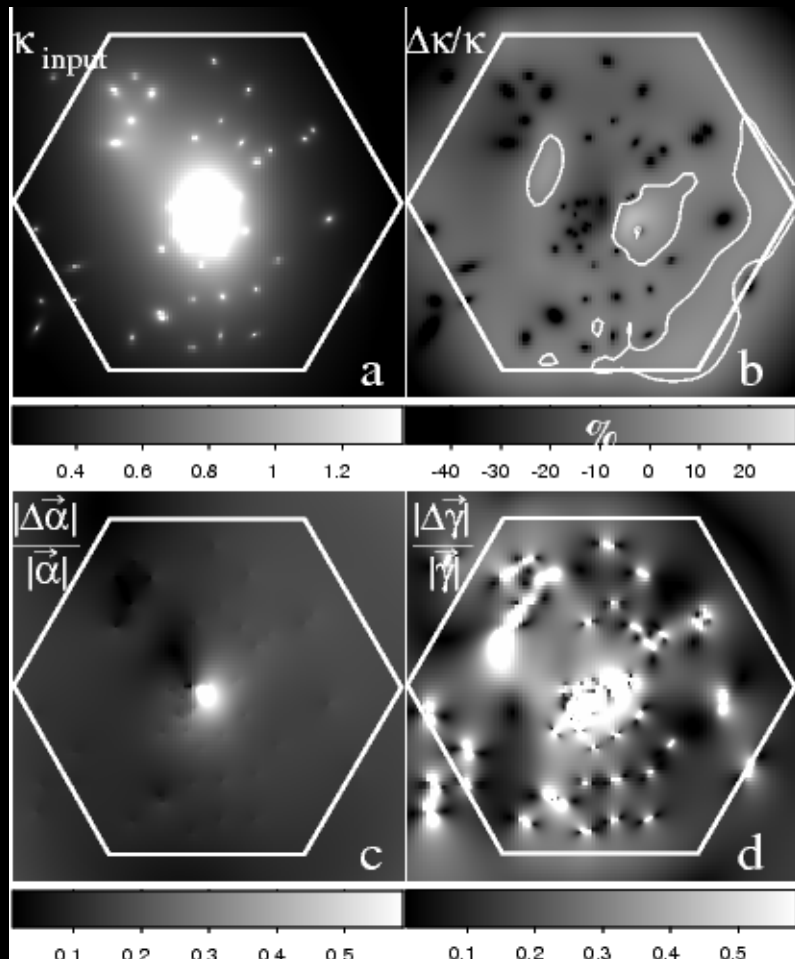
ACS field of A1689

Hexagonal limits and cristal-packed grid of nodes to match the natural shape of clusters

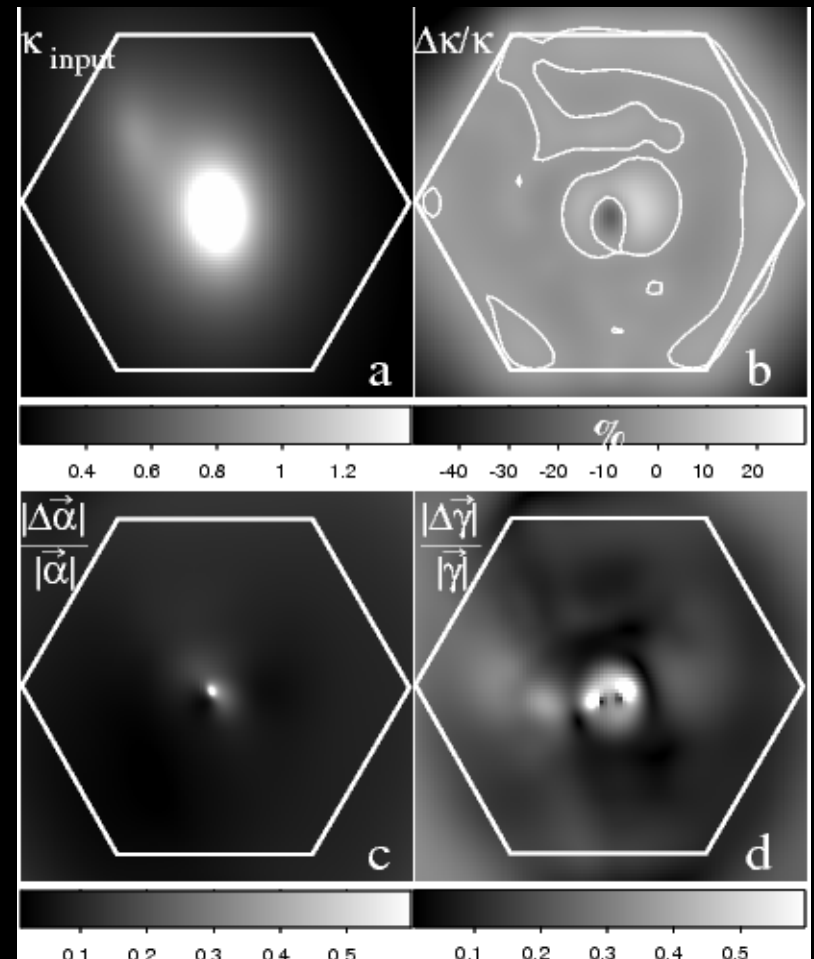
Splitting of triangles according to a mass density threshold

PIEMD  $r_{\text{cut}}/r_{\text{core}} = 3$  is a good ratio

# Adaptative grid model

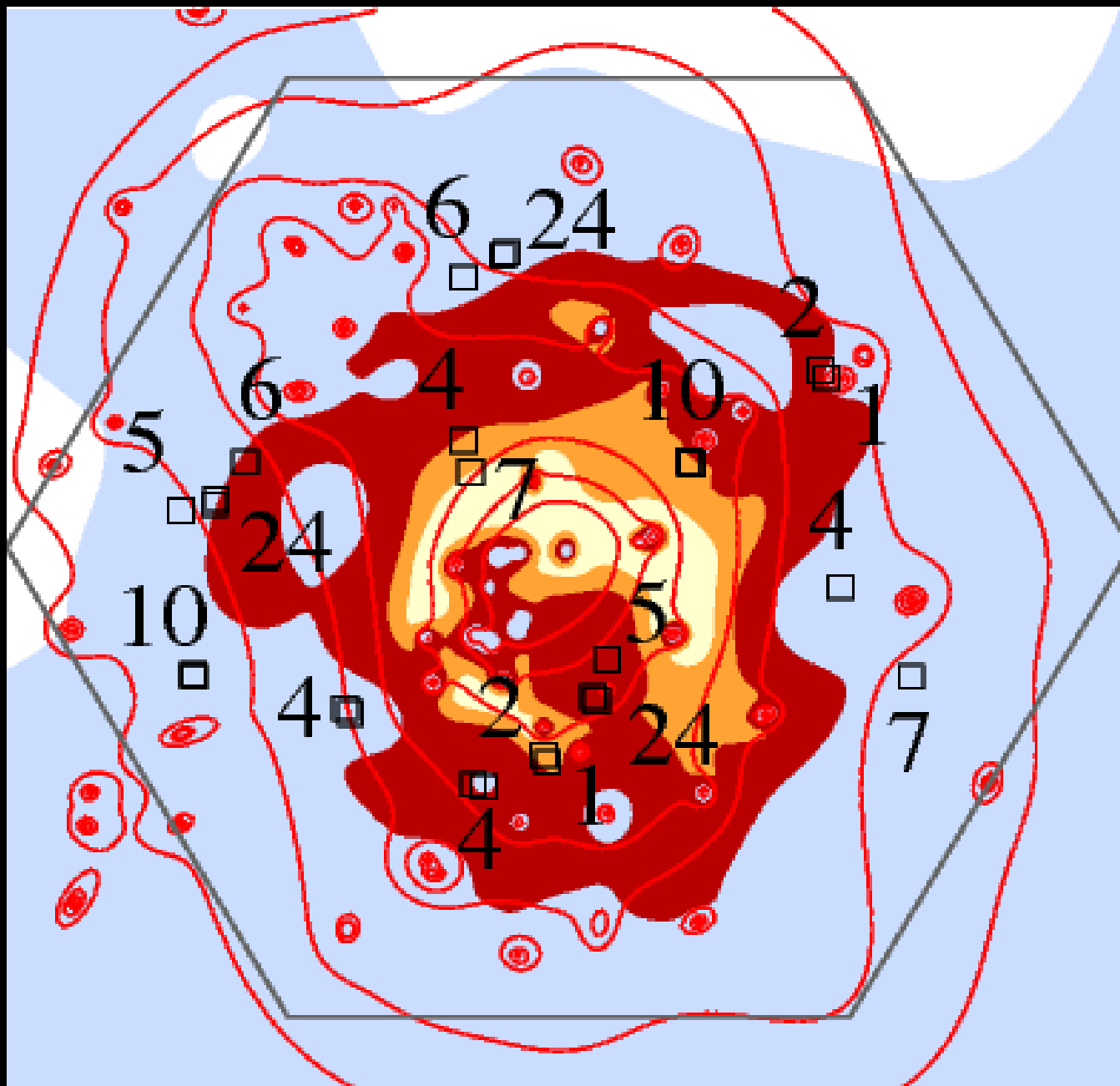


Adaptive grid alone - Input model



(Adaptive grid + galaxy scale halos) - Input Model

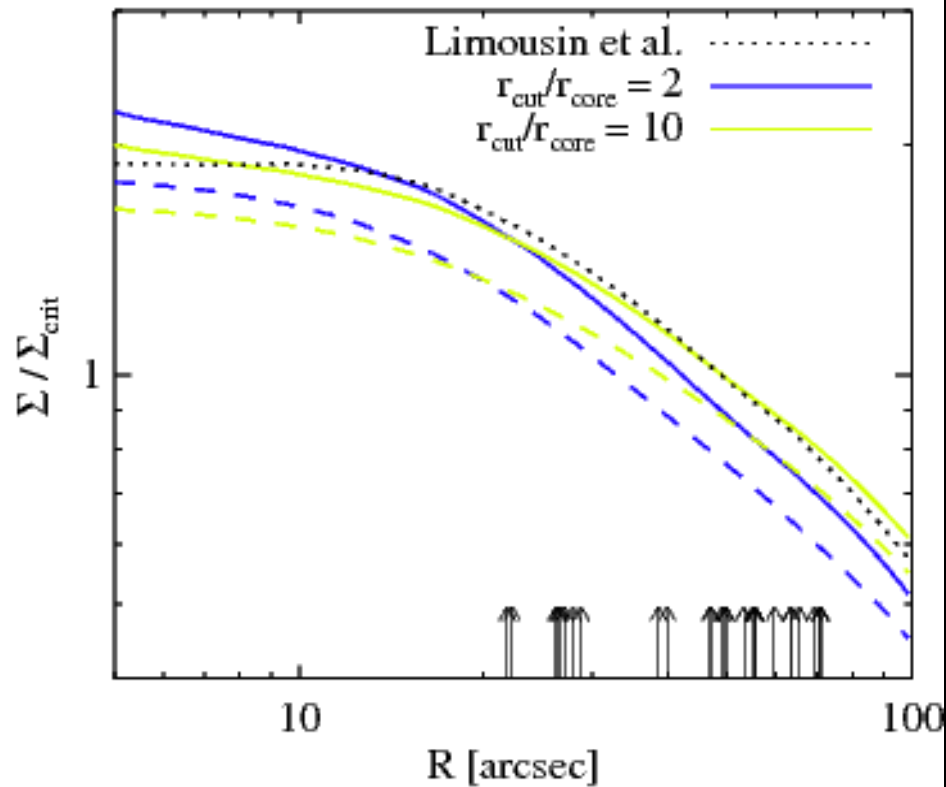
# Mass map + Error estimation



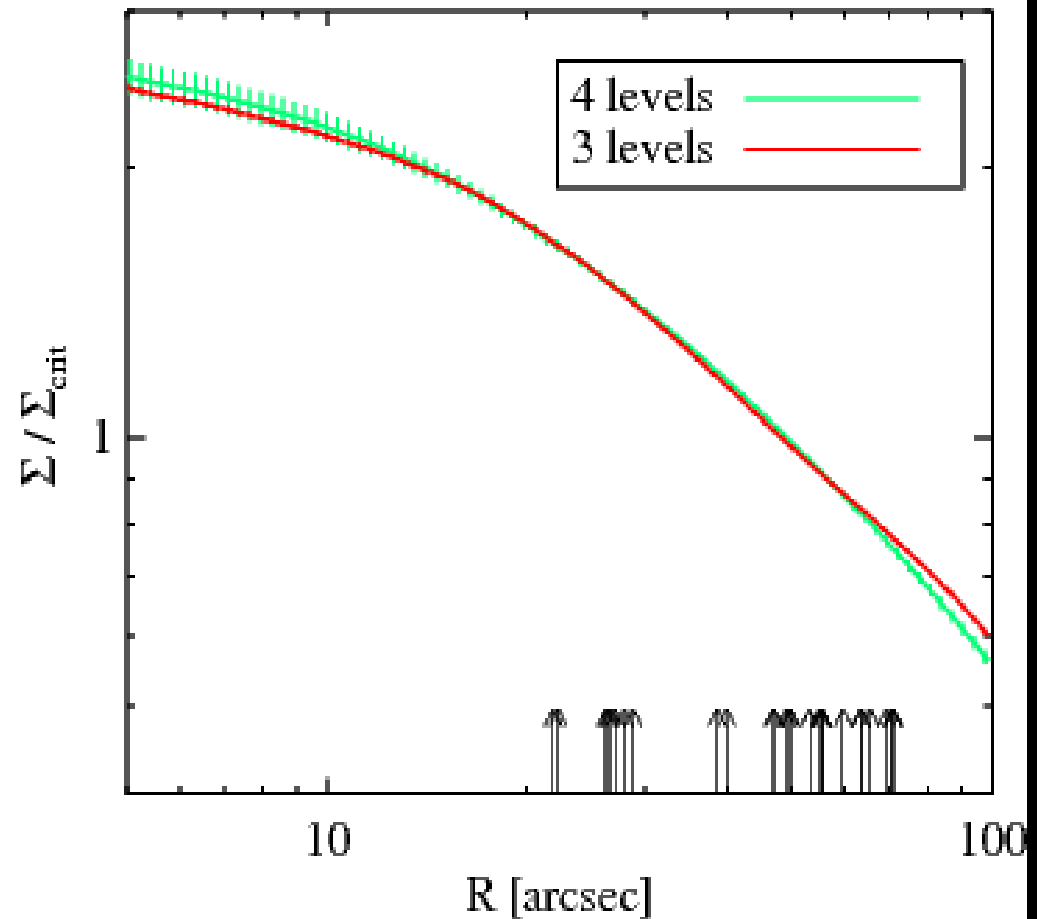
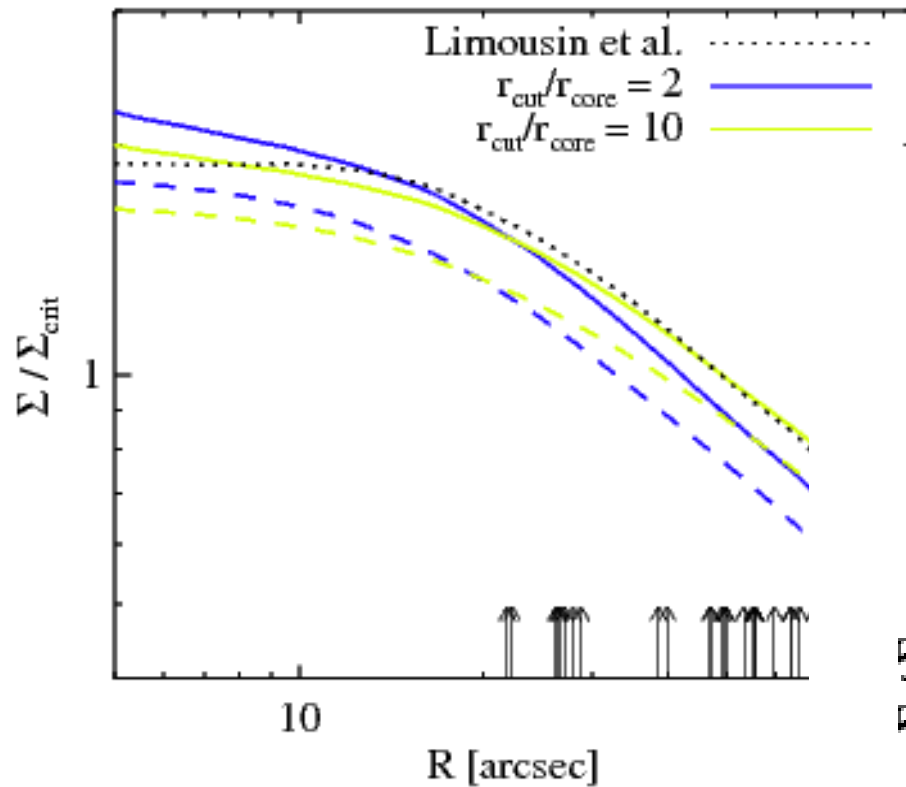
With 3 levels of  
splitting  
 $r_{\text{cut}}/r_{\text{core}}=3$

12 systems of  
multiple images

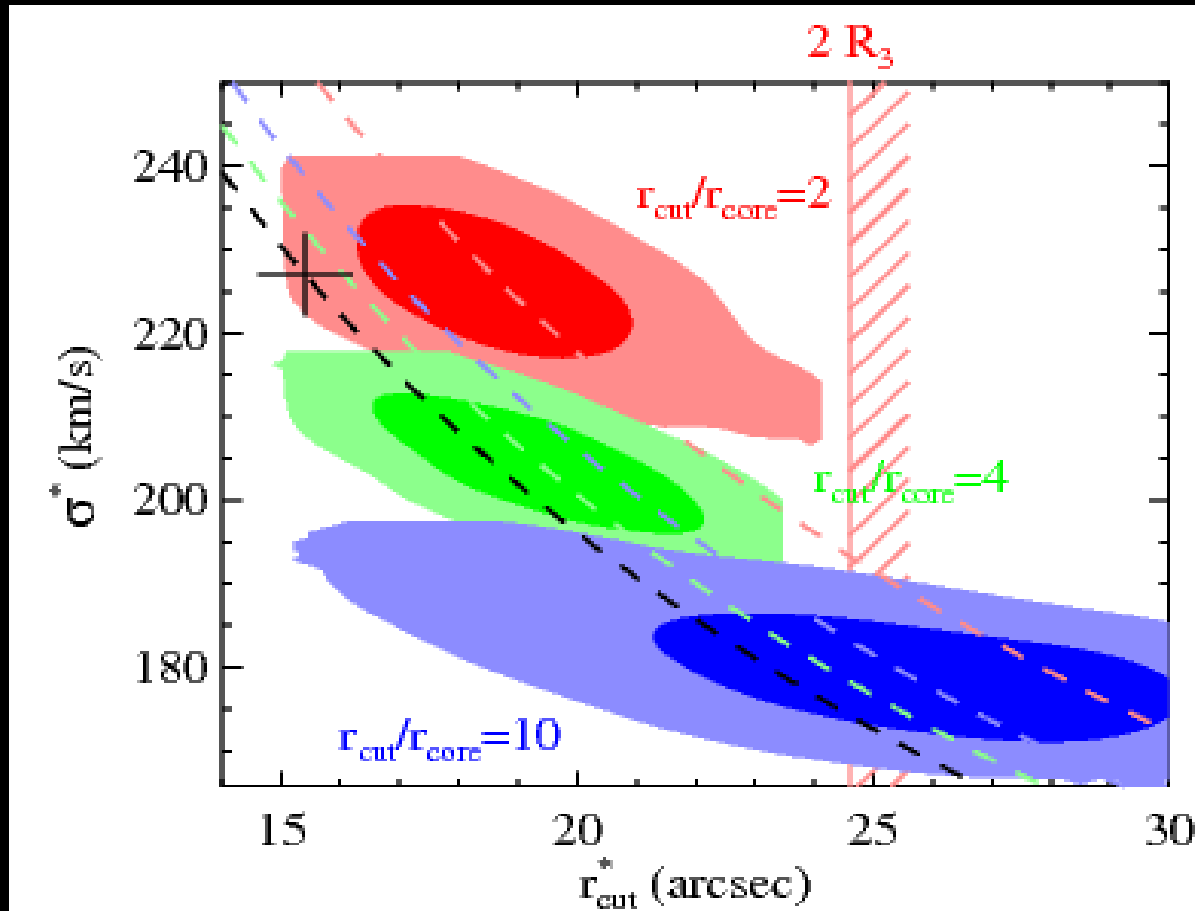
# Systematics due to non parametric parameters



# Systematics due to non parametric parameters

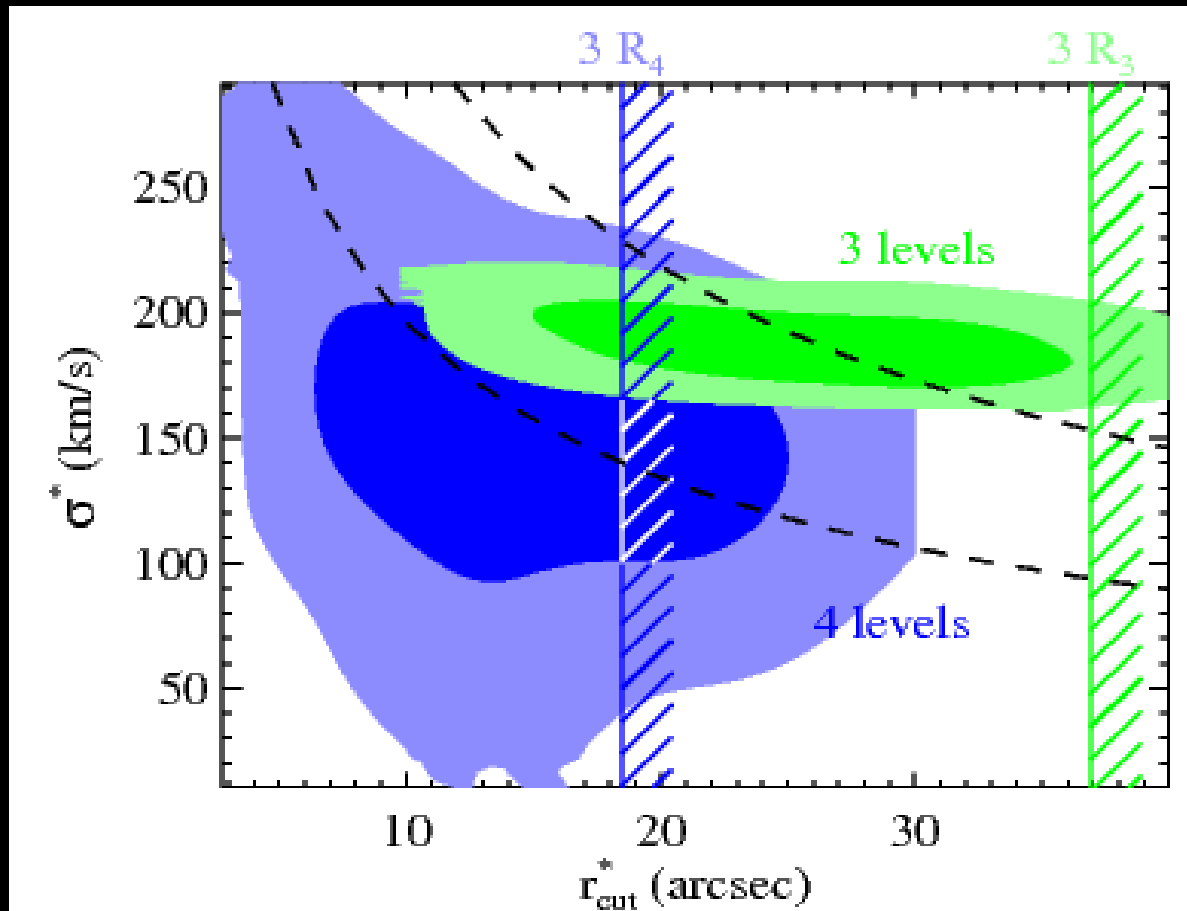


# Degeneracies between grid & subst.



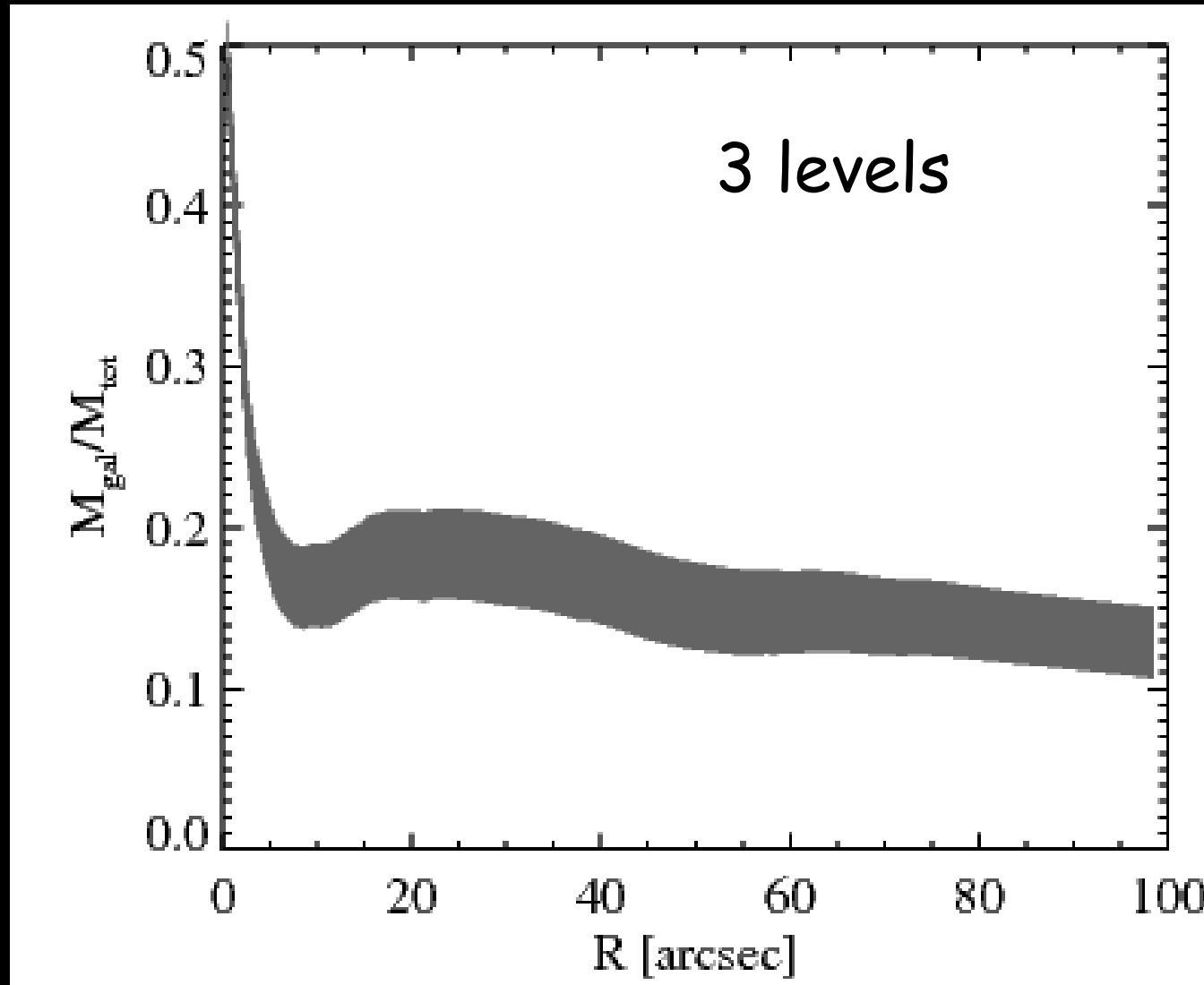


# Degeneracies between grid & subst.

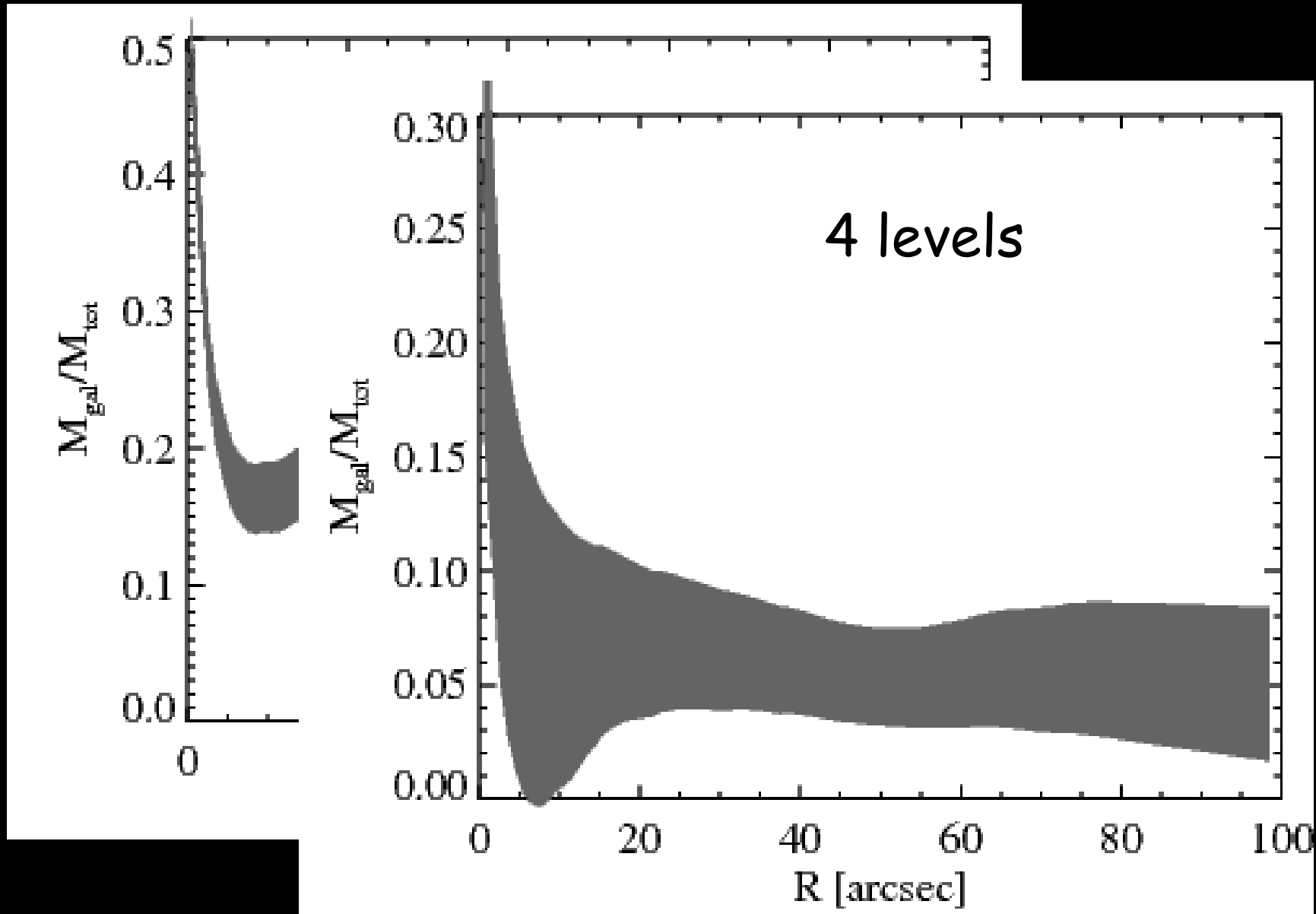


→ Hard to estimate with confidence the mass of subst.

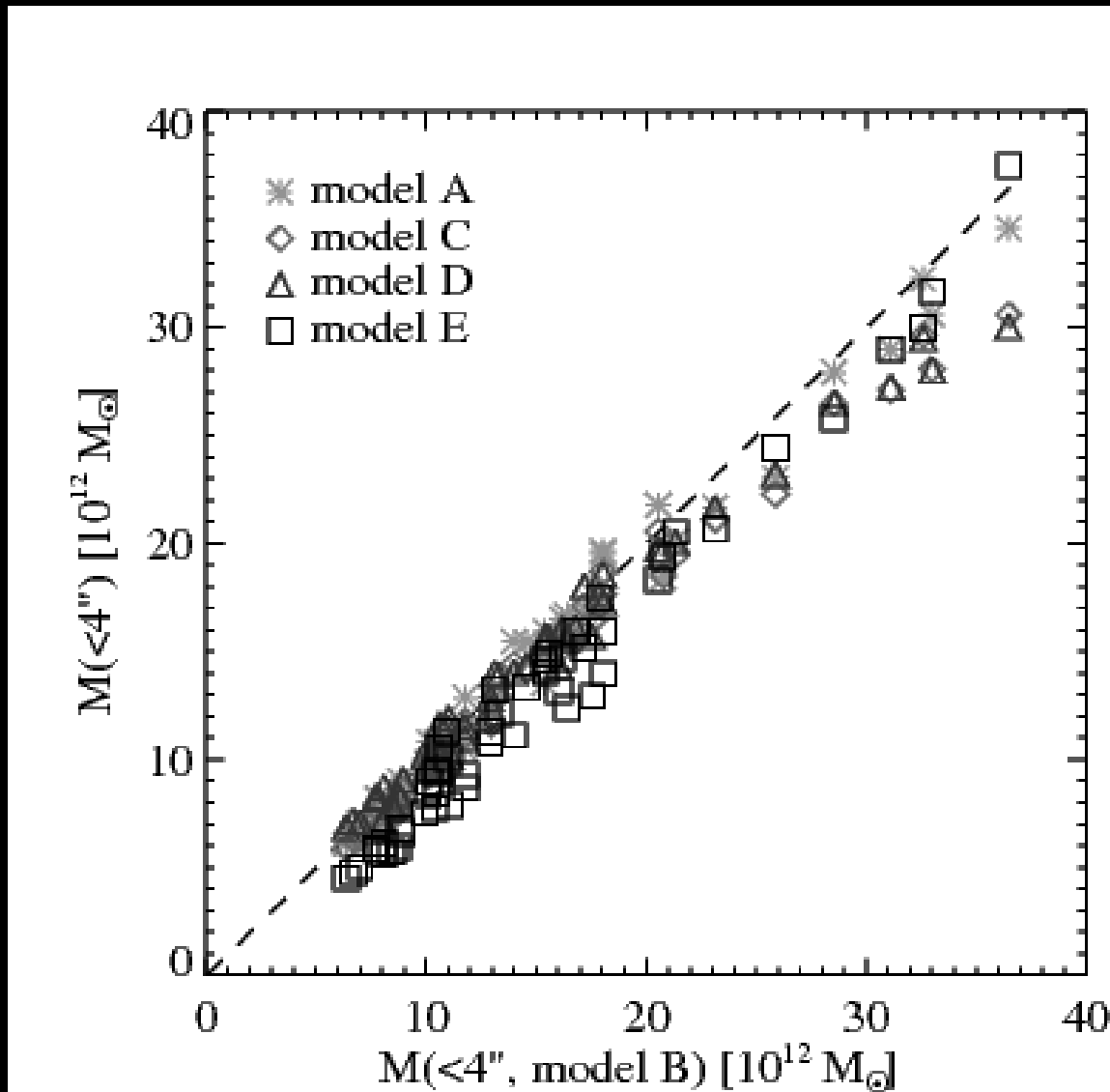
# Overall with grid models



# Overall with grid models



# Invariant quantity



Aperture mass around  
observed galaxies

# Future applications of grid modelling

- Straightforward combination WL + SL thanks to :
  - adaptive grid
  - Analytic potentials → forward fitting technique in which we do not linearize lensing equation (WL)
- Try to map the mass in the COSMOS field
- Study the application of grid models to estimate cosmological parameters